

MAT8034: Machine Learning

Deep Reinforcement Learning

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https://fangkongx.github.io/Teaching/MAT8034/Spring2025/index.html

Part of slide credits: Weinan Zhang

Outline

- Deep RL Value methods
- Deep RL Policy methods

Function approximation for value and policy



What if we use deep neural networks directly to approximate these functions?

End-to-end reinforcement learning



Deep RL enables RL algorithms to solve complex tasks in an end-to-end manner.

Slide from Sergey Levine. http://rail.eecs.berkeley.edu/deeprlcourse/static/slides/lec-1.pdf

Deep RL



New challenges when we combine deep learning with RL?

- Value functions and policies become deep neural networks
- High-dimensional parameter space
- Difficult to train stably
- Prone to overfitting
- Requires large amounts of data
- High computational cost
- CPU-GPU workload balance

Value methods: DQN

Deep Q-Network (DQN)

- Uses a deep neural network to approximate Q(s,a)
 - \rightarrow Replaces the Q-table with a parameterized function for scalability
- The network takes state s as input, outputs Q-values for all actions a simultaneously



Volodymyr Mnih, Koray Kavukcuoglu, David Silver et al. Playing Atari with Deep Reinforcement Learning. NIPS 2013 workshop.

DQN (cont.)

- Intuition: Use a deep neural network to approximate Q(s,a)
 - Instability arises in the learning process
 - Samples {(s_t, a_t, s_{t+1}, r_t)} are collected sequentially and do not satisfy the i.i.d. assumption
 - Frequent updates of Q(s,a) cause instability
- Solutions: Experience replay
 - Store transitions $e_t = (s_t, a_t, s_{t+1}, r_t)$ in a replay buffer D Sample uniformly from D to reduce sample correlation
 - Dual network architecture: Use an evaluation network and a target network for improved stability

"Human-Level Control Through Deep Reinforcement Learning", Mnih, Kavukcuoglu, Silver et al. (2015)

Target network

- Target network Q_{θ} -(s, a)
 - Maintains a copy of the Q-network with older parameters θ^-
 - Parameters θ^- are updated periodically (every C steps) to match the evaluation network
- Loss Function (at iteration i)

$$L_{i}(\theta_{i}) = \mathbb{E}_{s_{t},a_{t},s_{t+1},r_{t},p_{t}\sim D} \left[\frac{1}{2} \omega_{t}(r_{t} + \gamma \max_{a'} Q_{\theta_{i}^{-}}(s_{t+1},a') - Q_{\theta_{i}}(s_{t},a_{t}))^{2} \right]$$

"Human-Level Control Through Deep Reinforcement Learning", Mnih, Kavukeuoglu, Silver et al. (2015)

DQN training procedure

- Collect transitions using an ε-greedy exploration policy
 - Store $\{(s_t, a_t, s_{t+1}, r_t)\}$ into the replay buffer
- Sample a minibatch of k transitions from the buffer
- Update networks:
 - Compute the target using the sampled transitions
 - Update the evaluation network Q_{θ}
 - Every C steps, synchronize the target network Q_θ with the evaluation network

"Human-Level Control Through Deep Reinforcement Learning", Mnih, Kavukcuoglu, Silver et al. (2015)

DQN performance in Atari games



"Human-Level Control Through Deep Reinforcement Learning", Mnih, Kavukcuoglu, Silver et al. (2015)

Overestimation in Q-Learning

Q-function overestimation

- The target value is computed as: $y_t = r_t + \gamma \max_{a'} Q_{\theta}(s_{t+1}, a')$
- The max operator leads to increasingly larger Q-values, potentially exceeding the true value
- Cause of overestimation

$$\max_{a' \in A} Q_{\theta'}(s_{t+1}, a') = Q_{\theta'}(s_{t+1}, \arg \max_{a'} Q_{\theta'}(s_{t+1}, a'))$$

The chosen action might be overestimated due to Q-function error

Degree of overestimation in DQN

Overestimation increases with the number of candidate actions



A separately trained Q'-function is used as a reference

Overestimation example in DQN



- Setup: The x-axis represents states, and each plot includes 10 candidate actions. The purple curve denotes the true Q-value function, the green dots are training data points, and the green lines are the fitted Q-value estimates.
- The middle column shows the estimated values Q_t(s, a) for all 10 actions. After applying the max operator, the results deviate significantly from the true values Q_{*}(s, a).

Double DQN

 Uses two separate networks for action selection and value estimation, respectively.

DQN
$$y_t = r_t + \gamma Q_\theta(s_{t+1}, \arg \max_{a'} Q_\theta(s_{t+1}, a'))$$

Double DQN
$$y_t = r_t + \gamma Q_{\theta'}(s_{t+1}, \arg \max_{a'} Q_{\theta}(s_{t+1}, a'))$$

"Double Reinforcement Learning with Double Q-Learning", van Hasselt et al. (2016)

Experimental results in the Atari environment



Atari game performance

	no ops		human starts		
	DQN	DDQN	DQN	DDQN	DDQN
					(tuned)
Median	93%	115%	47%	88%	117%
Mean	241%	330%	122%	273%	475%

normalized performance

DQN score – random play score

= human score – random play score



Dueling DQN

Assume the action-value function follows a distribution:

 $Q(s,a) \sim \mathcal{N}(\mu,\sigma)$

• Then:
$$V(s) = \mathbb{E}[Q(s,a)] = \mu$$
 $Q(s,a) = \mu + \varepsilon(s,a)$

• How do we describe $\varepsilon(s, a)$?

$$\varepsilon(s,a) = Q(s,a) - V(s)$$

This term is also known as the Advantage function

"Dueling Network Architectures for Deep Reinforcement Learning", Wang et al. (2016)

Dueling DQN (cont.)

Advantage function

$$A^{\pi}(s,a) = Q^{\pi}(s,a) - V^{\pi}(s)$$

$$Q^{\pi}(s,a) = \mathbb{E}[R_t | s_t = s, a_t = a, \pi]$$

$$V^{\pi}(s) = \mathbb{E}_{a \sim \pi(s)}[Q^{\pi}(s, a)]$$

Different forms of advantage aggregation

$$Q(s,a;\theta,\alpha,\beta) = V(s;\theta,\beta) + (A(s,a;\theta,\alpha) - \max_{a' \in |A|} A(s,a';\theta,\alpha))$$

$$Q(s,a;\theta,\alpha,\beta) = V(s;\theta,\beta) + \left(A(s,a;\theta,\alpha) - \frac{1}{|A|} \sum_{a'} A(s,a';\theta,\alpha)\right)$$

Network structure



Advantages of Dueling DQN

- Effective for states weakly correlated with actions
- More efficient learning of the state-value function
 - The value stream V(s) is shared across all actions, allowing the network to generalize better across actions



saliency maps

•The value stream allows the agent to evaluate how good a state is without considering the specific action taken.

•The advantage stream emphasizes action-specific importance: for instance, it can learn to focus more when an obstacle (e.g., a car) appears in front of the agent, thereby guiding more precise action selection.

Experimental results in the Atari environment I



Experimental results in the Atari environment II



Deep RL – Policy-based methods

Review: The policy gradient theorem

- The policy gradient theorem generalizes the derivation of likelihood ratios to the multi-step MDP setting.
- It replaces the immediate reward r_t with the expected long-term return $Q^{\pi}(s, a)$.

$$\frac{\partial J(\theta)}{\partial \theta} = \mathbb{E}_{\pi_{\theta}} \left[\frac{\partial \log \pi_{\theta}(a|s)}{\partial \theta} Q^{\pi_{\theta}}(s,a) \right]$$

Policy network gradient

For stochastic policies, the probability of selecting an action is typically modeled using a softmax function:

$$\pi_{\theta}(a|s) = \frac{e^{f_{\theta}(s,a)}}{\sum_{a'} e^{f_{\theta}(s,a')}}$$

- $f_{\theta}(s, a)$ is a score function (e.g., logits) for the state-action pair
- Parameterized by θ , often realized via a neural network
- Gradient of the log-form

$$\begin{split} \frac{\partial \log \pi_{\theta}(a|s)}{\partial \theta} &= \frac{\partial f_{\theta}(s,a)}{\partial \theta} - \frac{1}{\sum_{a'} e^{f_{\theta}(s,a')}} \sum_{a''} e^{f_{\theta}(s,a'')} \frac{\partial f_{\theta}(s,a'')}{\partial \theta} \\ &= \frac{\partial f_{\theta}(s,a)}{\partial \theta} - \mathbb{E}_{a' \sim \pi_{\theta}(a'|s)} \left[\frac{\partial f_{\theta}(s,a')}{\partial \theta} \right] \end{split}$$

Policy network gradient (cont.)

Gradient of the log-form

$$\frac{\partial \log \pi_{\theta}(a|s)}{\partial \theta} = \frac{\partial f_{\theta}(s,a)}{\partial \theta} - \mathbb{E}_{a' \sim \pi_{\theta}(a'|s)} \left[\frac{\partial f_{\theta}(s,a')}{\partial \theta} \right]$$

Gradient of the policy network

$$\frac{\partial J(\theta)}{\partial \theta} = \mathbb{E}_{\pi_{\theta}} \left[\frac{\partial \log \pi_{\theta}(a|s)}{\partial \theta} Q^{\pi_{\theta}}(s,a) \right]$$
$$= \mathbb{E}_{\pi_{\theta}} \left[\left(\frac{\partial f_{\theta}(s,a)}{\partial \theta} - \mathbb{E}_{a' \sim \pi_{\theta}(a'|s)} \left[\frac{\partial f_{\theta}(s,a')}{\partial \theta} \right] \right) Q^{\pi_{\theta}}(s,a) \right]$$
Back propagation Back propagation

Comparison: DQN v.s. Policy gradient

Q-Learning:

- Learns a Q-value function $Q_{\theta}(s, a)$ parameterized by θ
- Objective: Minimize the TD error

$$J(\theta) = \mathbb{E}_{\pi'} \left[\frac{1}{2} \left(r_t + \gamma \max_{a'} Q_{\theta'}(s_{t+1}, a') - Q_{\theta}(s_t, a_t) \right)^2 \right]$$

$$\theta \leftarrow \theta - \alpha \frac{\partial J(\theta)}{\partial \theta}$$

$$= \theta + \alpha \mathbb{E}_{\pi'} \left[\left(r_t + \gamma \max_{a'} Q_{\theta'}(s_{t+1}, a') - Q_{\theta}(s_t, a_t) \right) \frac{\partial Q_{\theta}(s, a)}{\partial \theta} \right]$$

Comparison: DQN v.s. Policy gradient

- Q-Learning:
 - Learns a Q-value function $Q_{\theta}(s, a)$ parameterized by θ
 - Objective: Minimize the TD error

Policy gradient

- Learns a policy $\pi_{\theta}(a \mid s)$ directly, parameterized by θ
- Objective: Maximize the expected return directly

$$\max_{\theta} J(\theta) = \mathbb{E}_{\pi_{\theta}} [Q^{\pi_{\theta}}(s, a)]$$
$$\theta \leftarrow \theta + \alpha \frac{\partial J(\theta)}{\partial \theta} = \theta + \alpha \mathbb{E}_{\pi_{\theta}} \left[\frac{\partial \log \pi_{\theta}(a|s)}{\partial \theta} Q^{\pi_{\theta}}(s, a) \right]$$

Limitations of policy gradient methods

- Learning rate (step size) selection is challenging in policy gradient algorithms
 - Since the data distribution changes as the policy updates, a previously good learning rate may become ineffective.
 - A poor choice of step size can significantly degrade performance:
 - Too large \rightarrow policy diverges or collapses
 - Too small \rightarrow slow convergence or stagnation



Trust Region Policy Optimization (TRPO)

- Two forms of the optimization objective
 - Form 1: Trajectory-based objective $J(\theta) = \mathbb{E}_{\tau \sim p_{\theta}(\tau)}[\sum_{t} \gamma^{t} r(s_{t}, a_{t})]$
 - Form 2: State-value-based objective $J(\theta) = \mathbb{E}_{s_0 \sim p_{\theta}(s_0)}[V^{\pi_{\theta}}(s_0)]$

Optimization gap of the objective function



Importance sampling

$$J(\theta') - J(\theta) = \mathbb{E}_{\tau \sim p_{\theta'}(\tau)} \left[\sum_{t=0}^{\infty} \gamma^t A^{\pi_{\theta}}(s_t, a_t) \right]$$

$$= \sum_{t} \mathbb{E}_{s_t \sim p_{\theta'}(s_t)} [\mathbb{E}_{a_t \sim \pi_{\theta'}}(a_t | s_t) [\gamma^t A^{\pi_{\theta}}(s_t, a_t)]]$$

$$= \sum_{t} \mathbb{E}_{s_t \sim p_{\theta'}(s_t)} [\mathbb{E}_{a_t \sim \pi_{\theta}}(a_t | s_t) [\frac{\pi_{\theta'}(a_t | s_t)}{\pi_{\theta}(a_t | s_t)} \gamma^t A^{\pi_{\theta}}(s_t, a_t)]]$$

$$p_{\theta'}, \text{ approximation}$$
Importance sampling

Ignoring the difference in state distributions

- When the change between the old policy π_{θ} and the new policy $\pi_{\theta'}$ is small, we can approximate $p_{\theta}(s_t) \approx p_{\theta'}(s_t)$
 - For deterministic policies: The probability that $\pi_{\theta'}(s_t) \neq \pi_{\theta}(s_t)$ is less than a small threshold ϵ .
 - For stochastic policies:

The probability that $a' \sim \pi_{\theta'}(\cdot | s_t) \neq a \sim \pi_{\theta}(\cdot | s_t)$ is less than ϵ .

$$J(\theta') - J(\theta) \approx \sum_t \mathbb{E}_{s_t \sim p_{\theta}(s_t)} [\mathbb{E}_{a_t \sim \pi_{\theta}}(a_t | s_t) [\frac{\pi_{\theta'}(a_t | s_t)}{\pi_{\theta}(a_t | s_t)} \gamma^t A^{\pi_{\theta}}(s_t, a_t)]]$$

TRPO Policy Constraint

Use KL divergence to constrain policy update magnitude:

$$\begin{split} \theta' &\leftarrow \arg \max_{\theta'} \sum_{t} \mathbb{E}_{s_t \sim p_{\theta}(s_t)} [\mathbb{E}_{a_t \sim \pi_{\theta}}(a_t | s_t) [\frac{\pi_{\theta'}(a_t | s_t)}{\pi_{\theta}(a_t | s_t)} \gamma^t A^{\pi_{\theta}}(s_t, a_t)]] \\ \text{such that } \mathbb{E}_{s_t \sim p_{\theta}(s_t)} [D_{KL} \big(\pi_{\theta'}(a_t | s_t) \parallel \pi_{\theta}(a_t | s_t) \big)] \leq \epsilon \end{split}$$

In practice: use penalized objective with KL divergence penalty instead of hard constraint

$$\begin{aligned} \theta' \leftarrow \arg \max_{\theta'} \quad & \sum_{t} \mathbb{E}_{s_t \sim p_{\theta}(s_t)} [\mathbb{E}_{a_t \sim \pi_{\theta}}(a_t|s_t) [\frac{\pi_{\theta'}(a_t|s_t)}{\pi_{\theta}(a_t|s_t)} \gamma^t A^{\pi_{\theta}}(s_t, a_t)]] \\ & -\lambda(D_{KL}(\pi_{\theta'}(a_t|s_t) \parallel \pi_{\theta}(a_t|s_t)) - \epsilon) \end{aligned}$$

• Update θ' and $\lambda \leftarrow \lambda + \alpha(D_{KL}(\pi_{\theta'}(a_t|s_t) \parallel \pi_{\theta}(a_t|s_t)) - \epsilon)$

TRPO Monotonic Improvement Guarantee

$$J(\theta') \geq L_{\theta}(\theta') - C \cdot D_{KL}^{max}(\theta, \theta'), where C = \frac{4\epsilon\gamma}{(1-\gamma)^2}, \epsilon = \max_{s,a} |A_{\pi}(s,a)|$$

$$L_{\theta}(\theta') = J(\theta) + \sum_{t} \mathbb{E}_{s_t \sim p_{\theta}(s_t)} [\mathbb{E}_{a_t \sim \pi_{\theta}}(a_t|s_t) [\frac{\pi_{\theta'}(a_t|s_t)}{\pi_{\theta}(a_t|s_t)} \gamma^t A^{\pi_{\theta}}(s_t,a_t)]]$$

$$J(\theta')$$

$$I(\theta) = L(\theta) - C \cdot \mathsf{KL} \qquad \mathsf{L}(\theta)$$

Principle of TRPO



Gradient Ascent

Optimization in Trust Region

TRPO Drawbacks

Use KL divergence to constrain policy update magnitude:

$$\theta' \leftarrow \arg \max_{\theta'} \sum_{t} \mathbb{E}_{s_t \sim p_{\theta}(s_t)} [\mathbb{E}_{a_t \sim \pi_{\theta}}(a_t|s_t) [\frac{\pi_{\theta'}(a_t|s_t)}{\pi_{\theta}(a_t|s_t)} \gamma^t A^{\pi_{\theta}}(s_t, a_t)]]$$
such that $\mathbb{E}_{s_t \sim p_{\theta}(s_t)} [D_{KL} (\pi_{\theta'}(a_t|s_t) \parallel \pi_{\theta}(a_t|s_t))] \le \epsilon$
In practice: use penalized objective with KL divergence penalty instead
of hard constraint

$$\theta' \leftarrow \arg \max_{\theta'} \sum_{t} \mathbb{E}_{s_t \sim p_{\theta}(s_t)} [\mathbb{E}_{a_t \sim \pi_{\theta}}(a_t|s_t) [\frac{\pi_{\theta'}(a_t|s_t)}{\pi_{\theta}(a_t|s_t)} \gamma^t A^{\pi_{\theta}}(s_t, a_t)]] -\lambda (D_{KL} (\pi_{\theta'}(a_t|s_t) \parallel \pi_{\theta}(a_t|s_t)) - \epsilon)$$
Update θ' and $\lambda \leftarrow \lambda + \alpha (D_{KL} (\pi_{\theta'}(a_t|s_t) \parallel \pi_{\theta}(a_t|s_t)) - \epsilon)$

- High variance from importance weights
- Difficult to solve constrained optimization

Proximal Policy Optimization (PPO)

Clipped Surrogate Objective

conservative policy iteration

$$L^{CPI}(\theta) = \widehat{\mathbb{E}}_t \left[\frac{\pi_{\theta}(a_t | s_t)}{\pi_{\theta_{\text{old}}}(a_t | s_t)} \hat{A}_t \right] = \widehat{\mathbb{E}}_t \left[\frac{r_t(\theta) \hat{A}_t}{r_t(\theta) \hat{A}_t} \right]$$

 $L^{CLIP}(\theta) = \widehat{\mathbb{E}}_t \left[\min\left(r_t(\theta) \hat{A}_t, \operatorname{clip}(r_t(\theta), 1 - \epsilon, 1 + \epsilon) \hat{A}_t \right) \right]$



PPO: improvement over TRPO

I.Clipped surrogate objective

conservative policy iteration $L^{CPI}(\theta) = \widehat{\mathbb{E}}_t \left[\frac{\pi_{\theta}(a_t|s_t)}{\pi_{\theta_{\text{old}}}(a_t|s_t)} \hat{A}_t \right] = \widehat{\mathbb{E}}_t \left[\frac{r_t(\theta) \hat{A}_t}{r_t(\theta) \hat{A}_t} \right]$

 $L^{CLIP}(\theta) = \widehat{\mathbb{E}}_t \left[\min\left(r_t(\theta) \hat{A}_t, \operatorname{clip}(r_t(\theta), 1 - \epsilon, 1 + \epsilon) \hat{A}_t \right) \right]$

2.Generalized advantage estimation

 $\hat{A}_{t} = -V(s_{t}) + r_{t} + \gamma r_{t+1} + \dots + \gamma^{T-t+1} r_{T-1} + \gamma^{T-t} V(s_{T})$

 Use parallel actors to collect rollouts, compute advantage estimates, and update parameters with minibatches.

PPO: improvement over TRPO

3. Adaptive penalty parameter

$$L^{KLPEN}(\theta) = \widehat{\mathbb{E}}_t \left[\frac{\pi_{\theta}(a_t | s_t)}{\pi_{\theta_{\text{old}}}(a_t | s_t)} \widehat{A}_t - \frac{\beta \text{KL}[\pi_{\theta_{\text{old}}}(\cdot | s_t) | \pi_{\theta}(\cdot | s_t)]}{\pi_{\theta_{\text{old}}}(a_t | s_t)} \right]$$

- Adjust the penalty coefficient β dynamically:
 - Compute the KL value $d = \widehat{\mathbb{E}}_t \left| \text{KL} \left[\pi_{\theta_{\text{old}}}(\cdot | s_t) \middle| \pi_{\theta}(\cdot | s_t) \right] \right|$
 - If d < target / 1.5 $\rightarrow \beta \leftarrow \beta$ / 2
 - If d > target × 1.5 $\rightarrow \beta \leftarrow \beta \times 2$

Note: Here, 1.5 and 2 are empirical parameters, and the algorithm performance is not very sensitive to them

PPO experimental comparison

No clipping or penalty:

Clipping:

KL penalty (fixed or adaptive)

7 continuous control environments

3 random seeds

Each algorithm runs 100 episodes, repeated 21 times

Scores normalized to best model achieving 1.0

$$L_t(\theta) = r_t(\theta)\hat{A}_t$$

$$L_t(\theta) = \min(r_t(\theta)\hat{A}_t, \operatorname{clip}(r_t(\theta)), 1 - \epsilon, 1 + \epsilon)\hat{A}_t$$

$$L_t(\theta) = r_t(\theta)\hat{A}_t - \beta \operatorname{KL}[\pi_{\theta_{\text{old}}}, \pi_{\theta}]$$

algorithm	avg. normalized score
No clipping or penalty	-0.39
Clipping, $\epsilon = 0.1$	0.76
Clipping, $\epsilon = 0.2$	0.82
Clipping, $\epsilon = 0.3$	0.70
Adaptive KL $d_{\text{targ}} = 0.003$	0.68
Adaptive KL $d_{\text{targ}} = 0.01$	0.74
Adaptive KL $d_{\text{targ}} = 0.03$	0.71
Fixed KL, $\beta = 0.3$	0.62
Fixed KL, $\beta = 1$.	0.71
Fixed KL, $\beta = 3$.	0.72
Fixed KL, $\beta = 10$.	0.69

PPO in MuJoCo



PPO in ChatGPT



PPO in GPT4

Previous:

"If intelligence is a cake, the bulk of the cake is self-supervised learning, the icing on the cake is supervised learning, and the cherry on the cake is reinforcement learning (RL)." — Yann LeCun head of Facebook AI



Now:

Accuracy on adversarial questions (TruthfulQA mc1) Accuracy



from GPT-4 Technical Report

PPO in O1

September 12, 2024

Learning to Reason with LLMs

We are introducing OpenAl o1, a new large language model trained with reinforcement learning to perform complex reasoning. o1 thinks before it answers —it can produce a long internal chain of thought before responding to the user.

Contributions

GRPO in deepseek

Group Relative Policy Optimization In order to save the training costs of RL, we adopt Group Relative Policy Optimization (GRPO) (Shao et al., 2024), which foregoes the critic model that is typically the same size as the policy model, and estimates the baseline from group scores instead. Specifically, for each question q, GRPO samples a group of outputs { o_1, o_2, \dots, o_G } from the old policy $\pi_{\theta_{old}}$ and then optimizes the policy model π_{θ} by maximizing the following objective:

$$\mathcal{J}_{GRPO}(\theta) = \mathbb{E}[q \sim P(Q), \{o_i\}_{i=1}^G \sim \pi_{\theta_{old}}(O|q)]$$

$$\frac{1}{G} \sum_{i=1}^G \left(\min\left(\frac{\pi_{\theta}(o_i|q)}{\pi_{\theta_{old}}(o_i|q)} A_i, \operatorname{clip}\left(\frac{\pi_{\theta}(o_i|q)}{\pi_{\theta_{old}}(o_i|q)}, 1 - \varepsilon, 1 + \varepsilon\right) A_i\right) - \beta \mathbb{D}_{KL}\left(\pi_{\theta}||\pi_{ref}\right) \right), \quad (1)$$

$$\mathbb{D}_{KL}\left(\pi_{\theta}||\pi_{ref}\right) = \frac{\pi_{ref}(o_i|q)}{\pi_{\theta}(o_i|q)} - \log\frac{\pi_{ref}(o_i|q)}{\pi_{\theta}(o_i|q)} - 1, \quad (2)$$

where ε and β are hyper-parameters, and A_i is the advantage, computed using a group of rewards { $r_1, r_2, ..., r_G$ } corresponding to the outputs within each group:

$$A_{i} = \frac{r_{i} - \text{mean}(\{r_{1}, r_{2}, \cdots, r_{G}\})}{\text{std}(\{r_{1}, r_{2}, \cdots, r_{G}\})}.$$
(3)

Summary

- 1. Value-based deep RL
 - DQN
 - Double DQN
 - Dueling DQN
- 2. Policy-based RL
 - Policy gradient
 - TRPO
 - PPO
 - GRPO